

Exam 1, Fall 2005

Notes on Solution

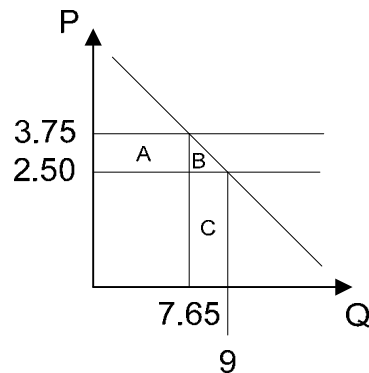
Part 1: Hurricanes and Gasoline

Note: The problem SHOULD have included the information on the number of gallons in a barrel but it did not. These results show what you would have obtained if you treated a gallon and a barrel as the same thing. In reality, there are 42 gallons in a barrel.

Elasticity:	-0.3
Percent change in Q:	-15
Initial Q:	9 million
Initial P:	2.5

Percentage change in P:	$-15 / -0.3$	=	50 percent
New P:	$2.5 * 1.5$	=	3.75 dollars
Change in Q:	$-0.15 * 9$	=	-1.35 million
New Q:	$9 - 1.35$	=	7.65 million

The diagram looks as follows:



Consumers lose areas A and B. Producers gain area A. B is DWL. What happens to area C depends on how you interpreted the problem. If you took \$2.50 to be the producers' W2A for gas, C was NOT part of PS before the hurricanes and is therefore NOT a loss to producers. On the other hand, if you treated the supply curves as perfectly vertical, which is consistent with a perfectly inelastic supply curve, C is a loss of PS. Either interpretation is OK. The true supply curve is between the two extremes: it is steep, but not perfectly vertical.

Computing the areas:

A:	7.65×1.25	=	\$	9.56	million per day
B:	$0.5 \times 1.35 \times 1.25$	=	\$	0.84	million per day
C:	$(9 - 7.65) \times 2.50$	=	\$	3.38	million per day

ΔCS	-A-B	=	\$	-10.41	million per day
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ΔPS (v1)	A	=	\$	9.56	million per day
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ΔPS (v2)	A-C	=	\$	6.19	million per day
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DWL (v1):	-B	=	\$	-0.84	million per day
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DWL (v2):	-B-C	=	\$	-4.22	million per day
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Over 28 Days:

ΔCS		=	\$	-291.38	million per month
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ΔPS (v1):		=	\$	267.75	million per month
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ΔPS (v2):		=	\$	173.25	million per month
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DWL (v1):		=	\$	-23.63	million per month
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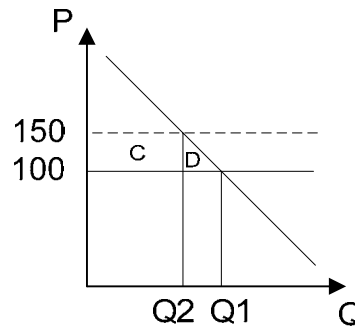
DWL (v2):		=	\$	-118.13	million per month
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Part 2: Taxes

P orig	\$	100
Tax	\$	50
P new	\$	150
% Δ P		50%

Group		A	B
η		-0.2	-1
Q1		1,000	1,000
% Δ Q	$\eta * \% \Delta P$	-10%	-50%
ΔQ	$\% \Delta Q * Q1$	-100	-500
Q2	$Q1 + \Delta Q$	900	500

ΔCS	C+D	\$	-47,500	\$	-37,500
Revenue	C	\$	45,000	\$	25,000
DWL	D	\$	-2,500	\$	-12,500
DWL/Rev	D/C	\$	-0.06	\$	-0.50



The tax is inefficient: it costs people more in lost CS than it raises in revenue. The inefficiency is particularly severe for group B: every dollar of revenue raised from it creates \$0.50 worth of DWL: that is, raising a dollar of tax revenue from group B costs the group \$1.50 in CS. The DWL per dollar is worst for group B because its demand is most elastic (-1.0 vs -0.2 for group A). The elastic demand means that the group is very sensitive to the price and cuts its consumption a lot under the tax.

Part 3: Demand and Supply

3a) initial equilibrium

$$W2P = 14000 - 5Q$$

$$W2A = 2000 + Q$$

$$W2P = W2A$$

$$14000 - 5Q = 2000 + Q$$

$$12000 = 6Q$$

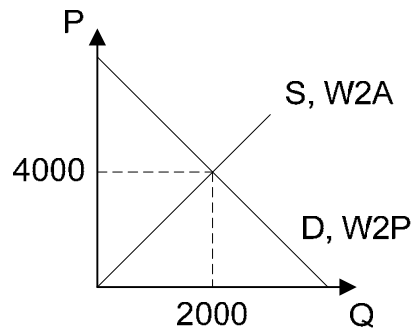
$$2000 = Q$$

$$W2P = 14000 - 5 \cdot 2000 = 4000$$

$$W2A = 2000 + 2000 = 4000$$

$$P = 4000$$

Graphing:



3b) equilibrium with a \$1200 subsidy

$$W2P = 14,000 - 5Q$$

$$W2A = 2000 + Q$$

At the new equilibrium:

$$W2P = P$$

$$W2A = P + 1200$$

$$W2A = W2P + 1200$$

$$W2P + 1200 = W2A$$

$$14,000 - 5Q + 1200 = 2000 + Q$$

$$13,200 = 6Q$$

$$2200 = Q$$

$$W2P = 14,000 - 5 \cdot 2200 = 3000$$

$$W2A = 2000 + 2200 = 4200$$

Purchaser price: 3000

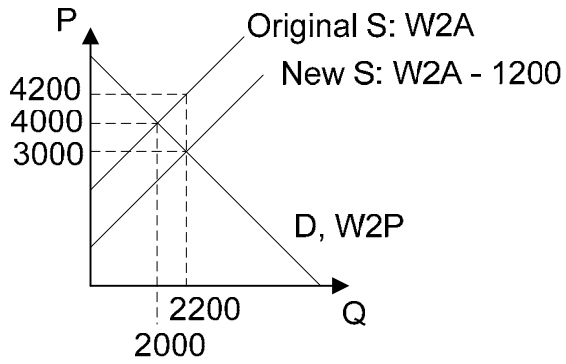
Producer price: 4200

Quantity: 2200

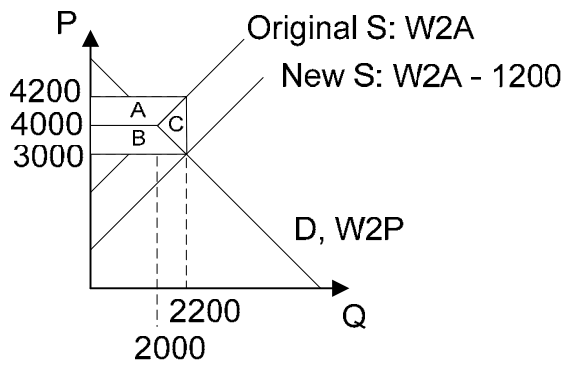
buyers purchase until $W2P = P$
sellers supply as until $W2A = P + \text{subsidy}$
combining: sellers sell until $W2A = W2P + \text{subsidy}$

3c) Diagram

The market equilibrium:



Redrawing the diagram to show changes in surplus more clearly (a single diagram was sufficient for the exam):



Change in CS: +B

Change in PS: +A

Change in government revenue: $-(A+B+C)$

Deadweight loss: C

Part 4: Rent Control

Initial equilibrium and elasticities:

P1	\$	1,000
Q1		25,000
η_d		-0.5
η_s		1.0

P2 \$ 800 rent control price

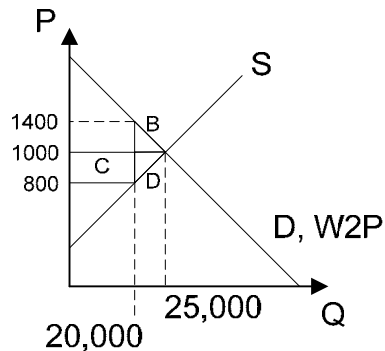
Change in apartments supplied by landlords:

$\% \Delta P$		-20%
$\% \Delta Q$	$\eta_s * \% \Delta P$	-20%
ΔQ	$\% \Delta Q * Q1$	-5000
Q2	$Q1 + \Delta Q$	20,000

To calculate the full effects of the policy, we need to calculate the height of the demand curve at 20,000 apartments. That's easy to do using the percentage change in quantity and the elasticity of demand:

$\% \Delta Q$		-20%
$\% \Delta P$	$\% \Delta Q / \eta_d$	40% price change needed to drive quantity demanded down
ΔP	$P1 * \% \Delta P$	\$ 400
P2	$P1 + \Delta P$	\$ 1,400 W2P of person who gets the last apartment (20,000)

Diagram:



Effect on surplus:

B		\$ 1,000,000
C		\$ 4,000,000
D		\$ 500,000
ΔCS	$-B + C$	\$ 3,000,000
ΔPS	$-C - D$	\$ -4,500,000
DWL	$-B - D$	\$ -1,500,000