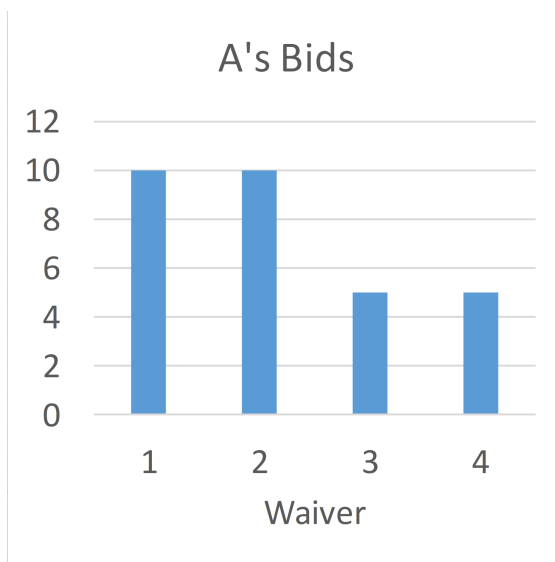


Individual Demand

Start by graphing **WTP** bids for person A:

Waiver	WTP
1	10
2	10
3	5
4	5



Height: WTP for a particular waiver

$WTP(Q) =$ WTP for waiver number Q

A's WTP for waiver 2 is $WTP_A(2) = 10$

A's WTP for waiver 3 is $WTP_A(3) = 5$

WTP for several waivers?

Add up WTP's for individual waivers

WTP for N waivers:

$$\sum_i^N \text{WTP}(Q_i)$$

Example: A's WTP for waivers 1 & 2

$$\text{WTP}_A(1) + \text{WTP}_A(2) = 10 + 10 = 20$$

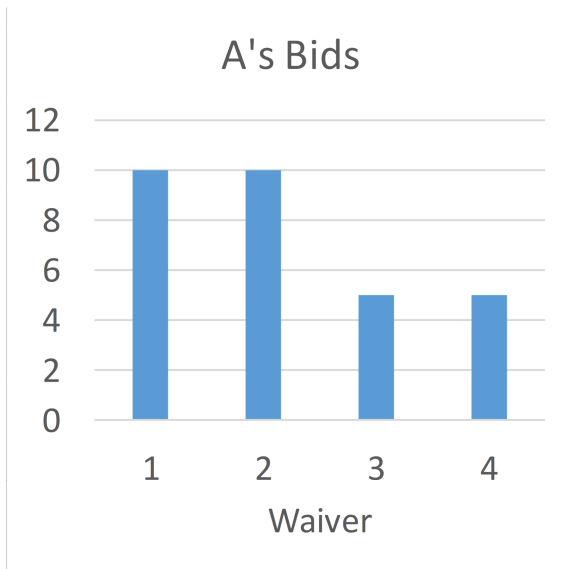
Can also find quantity A would **buy** at a given price P :

A's decision rules:

1. Buy any units with $\text{WTP}_A > P$ (net gain)
2. Buy any units with $\text{WTP}_A = P$ (indifferent)
3. Don't buy units with $\text{WTP}_A < P$

Result: A's *demand* at P

Example: suppose $P = 6$:



Applying decision rules:

Waiver	WTP	P	Net	Buy?
1	10	6	+4	Yes
2	10	6	+4	Yes
3	5	6	-1	No
4	5	6	-1	No

Gain on purchased waivers is consumer surplus (CS):

Consumer surplus (CS) on a single waiver i :

$$CS_i = WTP_i - P$$

$$\text{Person A, waivers 1 and 2: } CS_1 = 4, CS_2 = 4$$

Consumer surplus on purchase of N waivers:

$$CS = \sum_i^N CS_i$$

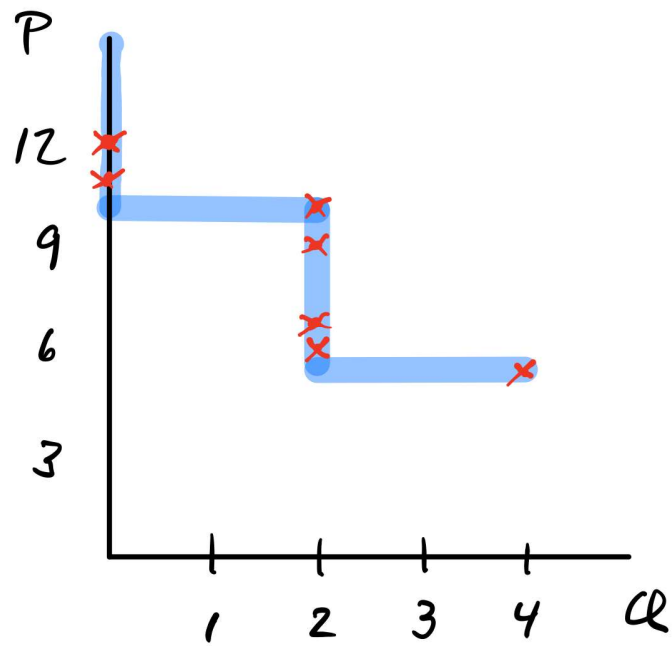
$$\text{Person A, total: } CS = CS_1 + CS_2 = 4 + 4 = 8$$

Demand *curve* is Q demanded for each possible P:

- Start at high price and sweep down axis:



P	Q
12	0
11	0
10	2
9	2
...	
7	2
6	2
5	4
...	



Third use of data beyond $WTP(Q)$ and $Q^D(P)$:

Marginal benefit (MB) of *giving* someone a unit

Take to be equal to what they would have been WTP:

$$MB_i = WTP_i$$

Giving person A waiver 1: $MB_1 = 10$

Market Demand

Market demand is the sum of individual demands:

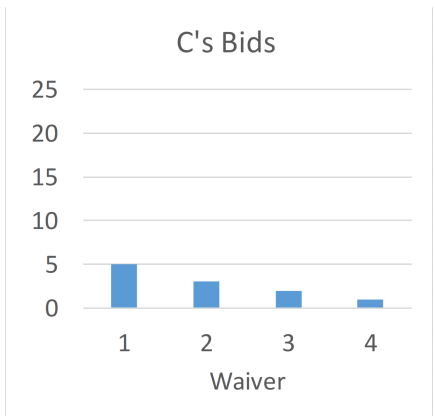
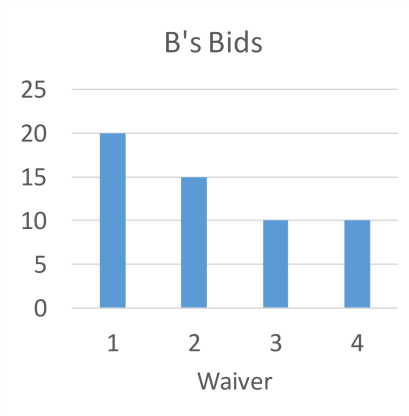
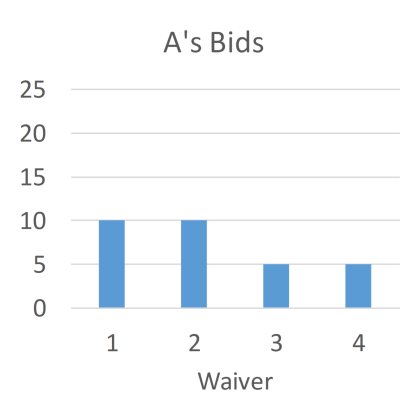
$$Q_M^D = \sum_i^N Q_i^D(P)$$

⚠ Sum of Qs, not WTPs ⚠

Computing for three people: A, B and C:

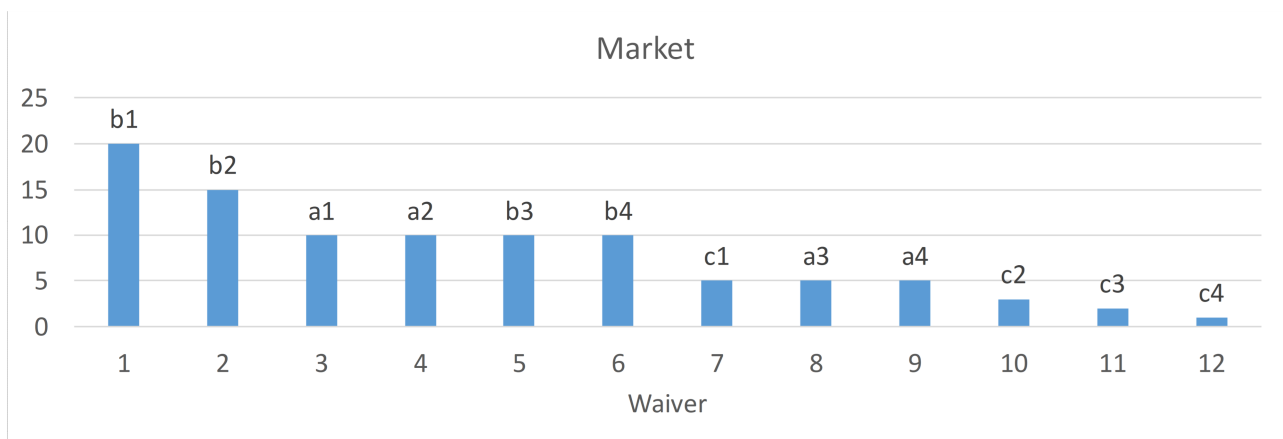
Individual WTP data:

Waiver	WTP_A	WTP_B	WTP_C
1	10	20	5
2	10	15	3
3	5	10	2
4	5	10	1



Market demand:

- As before, start with high prices and sweep down
- Count individual waivers demanded at each price
- In effect, lists bids from highest to lowest



Height of curve at given Q is WTP:

$$WTP_M(Q_i) = \text{WTP by the buyer of unit } Q_i$$

Examples:

- Waiver 2 (b2) has $WTP_M(2) = 15$
- Waiver 6 (b4) has $WTP_M(6) = 10$

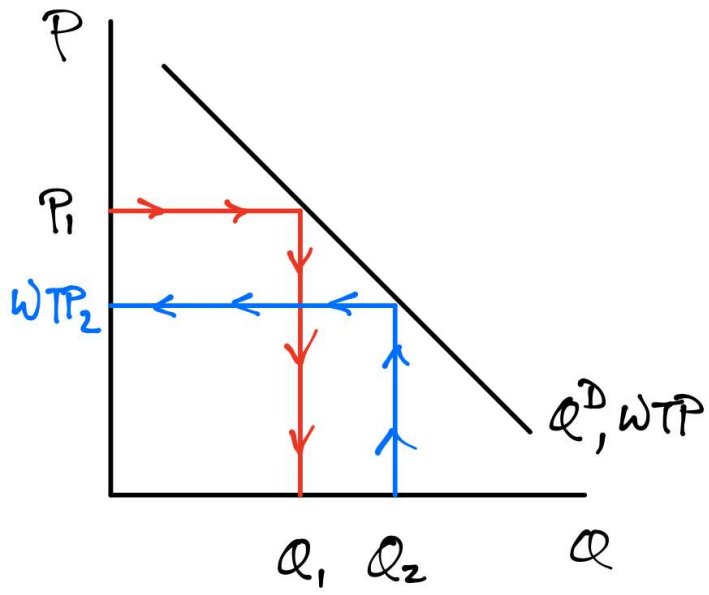
Width of curve at a given P is demand:

$$Q_M^D(P) = \text{quantity demanded at a given } P$$

Examples:

- At $P = 12$, $Q_M^D = 2$
- At $P = 9$, $Q_M^D = 6$

Abstract, stylized WTP and demand curve:



Red:

From P_1 can infer Q_1

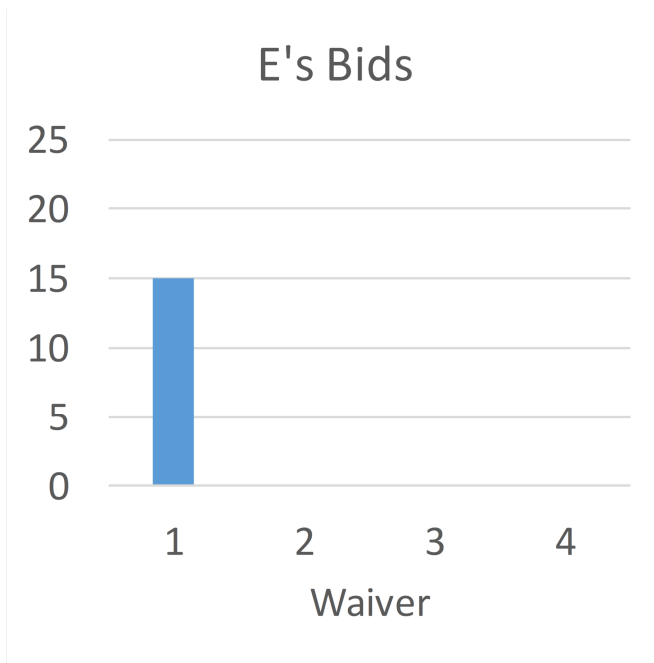
Blue:

From Q_2 can infer WTP_2

Individual Supply

Start by graphing **WTA** bids for person E:

Waiver	WTA
1	15



Height: **WTA** for the waiver

E's WTA for waiver is $WTA_E(1) = 15$

Can also find quantity E would **sell** at a given price P :

E's decision rules:

1. Sell if $P > WTA_E$ (net gain)
2. Sell if $P = WTA_E$ (indifferent)
3. Don't sell if $P < WTA_E$

Result: E's supply at P

Example: suppose $P = 20$

$$P = \$20$$

$$WTA_E(1) = \$15$$

Would sell 1 waiver

Gain on sold waivers is producer surplus (PS)

Producer surplus (PS) on a single waiver i :

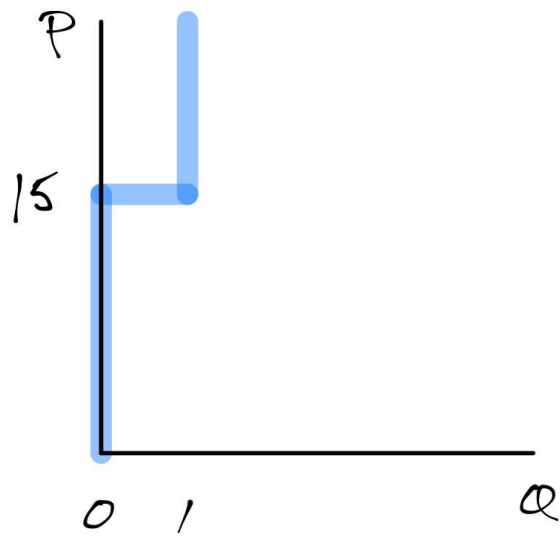
$$PS_i = P - WTA_i$$

$$\text{E's surplus: } PS_1 = \$20 - \$15 = \$5$$

Producer surplus on sales of N waivers:

$$PS = \sum_i^N PS_i$$

Supply curve is the Q supplied for each possible P :



If $P \geq 15$:
 $Q = 1$

If $P < 15$:
 $Q = 0$

Market Supply

Market supply is the sum of individual supplies:

$$Q_M^S = \sum_i^N Q_i^S(P)$$

⚠ Sum of Qs, not WTAs ⚠

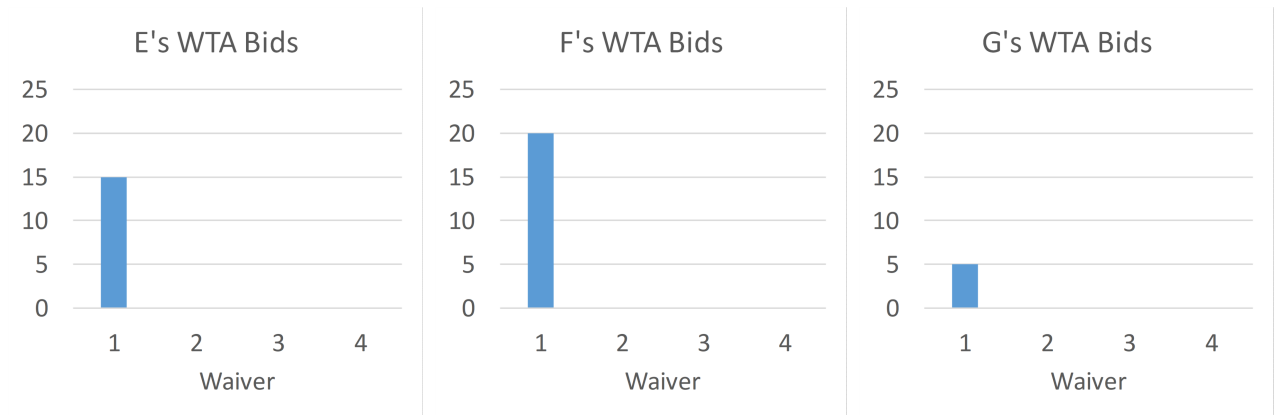
Extracting 2 more WTA bids:

$$WTA_E = \$15$$

$$WTA_F = \$20$$

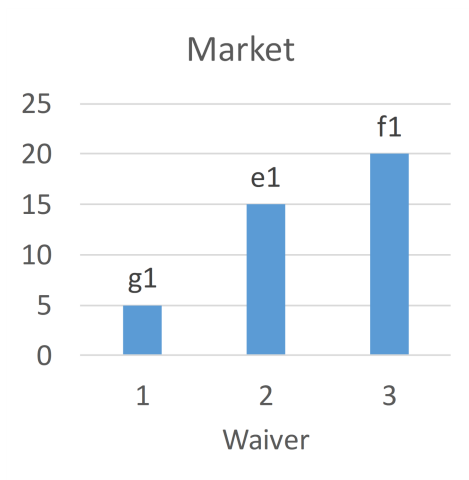
$$WTA_G = \$5$$

Individual supplies:



Market supply:

- Here, start with low prices and sweep up
- Count individual waivers supplied at each price
- In effect, lists bids from lowest to highest



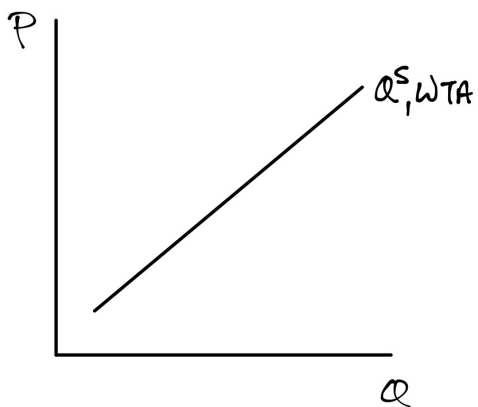
Height of curve:

$$WTA_M(Q_i) = \text{WTA by the seller of unit } Q_i$$

Width of curve:

$$Q_M^S(P) = \text{quantity supplied at a given } P$$

Abstract, stylized WTA and supply curve:



Market Equilibrium

Now have market demand and supply:

Demand	Supply
$Q_M^D(P)$	$Q_M^S(P)$

Give Q^D and Q^S for every possible price P

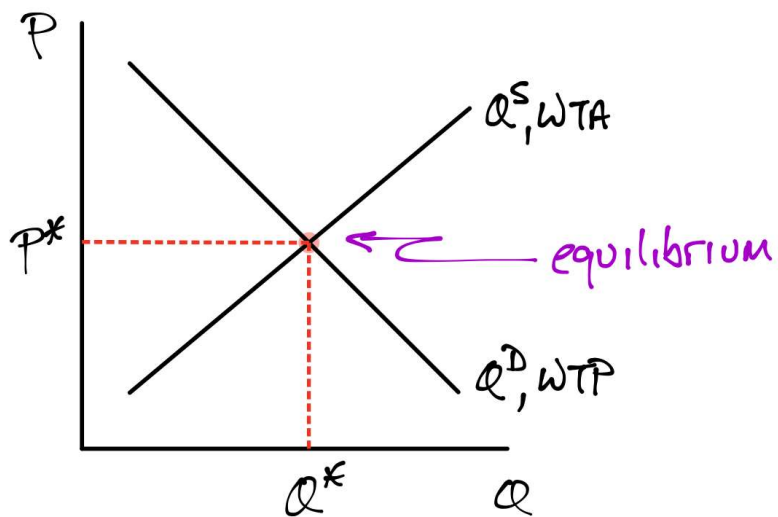
Can use to find *equilibrium price* P^* where Q s are equal:

Solve for P^* that makes $Q_M^D(P^*) = Q_M^S(P^*)$

Corresponding Q is the *equilibrium quantity* Q^* :

$$Q_M^D(P^*) = Q_M^S(P^*) = Q^*$$

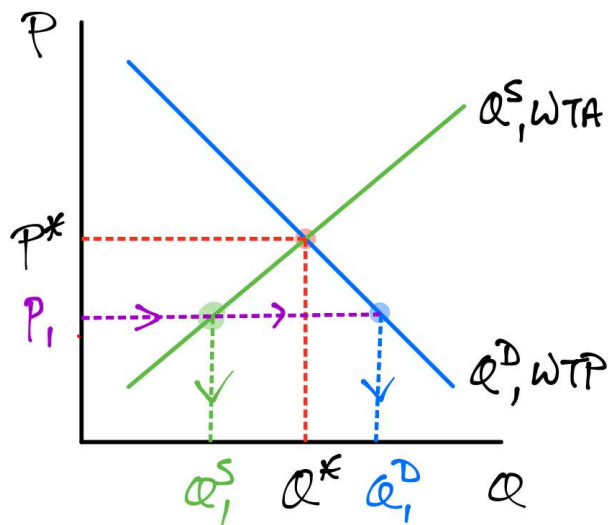
Graphically, the equilibrium is where the curves cross:



Equilibrium:

- P is *stable*: no forces pushing it up or down
- All other prices are **not** stable:

Case 1: P_1 below P^*



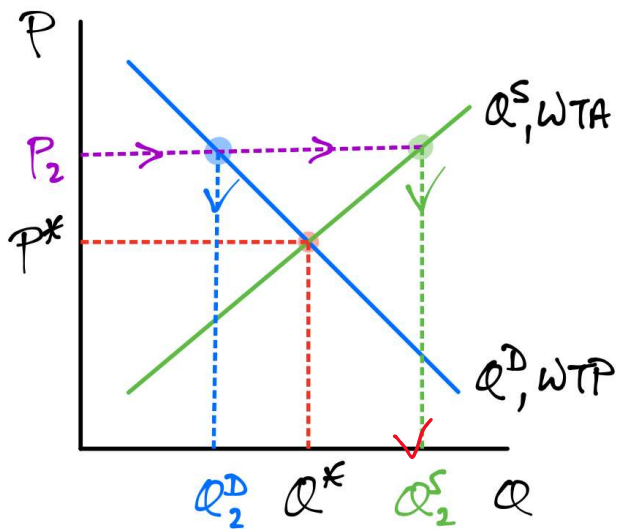
Buyers want more: $Q_M^D(P_1) > Q^*$

Sellers sell less: $Q_M^S(P_1) < Q^*$

$$Q_M^D(P_1) > Q_M^S(P_1)$$

- Excess **demand**
- Price will tend to **rise**

Case 2: P_2 above P^*



Buyers want less: $Q_M^D(P_2) < Q^*$

Sellers sell more: $Q_M^S(P_2) > Q^*$

$$Q_M^D(P_2) < Q_M^S(P_2)$$

- Excess **supply**
- Price will tend to **fall**

Finding P^* and Q^* algebraically:

Can solve either equation:

(I) Use demand = supply and solve for P^* first:

$$\text{Solve for } P^*: Q_M^D(P^*) = Q_M^S(P^*)$$

$$\text{Solve for } Q^*: Q^* = Q_M^D(P^*) \text{ or } Q^* = Q_M^S(P^*)$$

OR, (II) use $WTP = WTA$ and solve for Q^* first:

$$\text{Solve for } Q^*: WTP_M(Q^*) = WTA_M(Q^*)$$

$$\text{Solve for } P^*: P^* = WTP(Q^*) \text{ or } P^* = WTA(Q^*)$$